

ISSN 2518-170X (Online),  
ISSN 2224-5278 (Print)

ҚАЗАҚСТАН РЕСПУБЛИКАСЫ  
ҰЛТТЫҚ ҒЫЛЫМ АКАДЕМИЯСЫНЫҢ  
Қ. И. Сәтпаев атындағы Қазақ ұлттық техникалық зерттеу университеті

# Х А Б А Р Л А Р Ы

## ИЗВЕСТИЯ

НАЦИОНАЛЬНОЙ АКАДЕМИИ НАУК  
РЕСПУБЛИКИ КАЗАХСТАН  
Казакский национальный исследовательский  
технический университет им. К. И. Сатпаева

## NEWS

OF THE ACADEMY OF SCIENCES  
OF THE REPUBLIC OF KAZAKHSTAN  
Kazakh national research technical university  
named after K. I. Satpayev

### ГЕОЛОГИЯ ЖӘНЕ ТЕХНИКАЛЫҚ ҒЫЛЫМДАР СЕРИЯСЫ



### СЕРИЯ ГЕОЛОГИИ И ТЕХНИЧЕСКИХ НАУК



### SERIES OF GEOLOGY AND TECHNICAL SCIENCES

**6 (432)**

ҚАРАША – ЖЕЛТОҚСАН 2018 ж.  
НОЯБРЬ – ДЕКАБРЬ 2018 г.  
NOVEMBER – DECEMBER 2018

ЖУРНАЛ 1940 ЖЫЛДАН ШЫҒА БАСТАҒАН  
ЖУРНАЛ ИЗДАЕТСЯ С 1940 г.  
THE JOURNAL WAS FOUNDED IN 1940.

ЖЫЛЫНА 6 РЕТ ШЫҒАДЫ  
ВЫХОДИТ 6 РАЗ В ГОД  
PUBLISHED 6 TIMES A YEAR

---

---

*NAS RK is pleased to announce that News of NAS RK. Series of geology and technical sciences scientific journal has been accepted for indexing in the Emerging Sources Citation Index, a new edition of Web of Science. Content in this index is under consideration by Clarivate Analytics to be accepted in the Science Citation Index Expanded, the Social Sciences Citation Index, and the Arts & Humanities Citation Index. The quality and depth of content Web of Science offers to researchers, authors, publishers, and institutions sets it apart from other research databases. The inclusion of News of NAS RK. Series of geology and technical sciences in the Emerging Sources Citation Index demonstrates our dedication to providing the most relevant and influential content of geology and engineering sciences to our community.*

*Қазақстан Республикасы Ұлттық ғылым академиясы "ҚР ҰҒА Хабарлары. Геология және техникалық ғылымдар сериясы" ғылыми журналының Web of Science-тің жаңаланған нұсқасы Emerging Sources Citation Index-те индекстелуге қабылданғанын хабарлайды. Бұл индекстелу барысында Clarivate Analytics компаниясы журналды одан әрі the Science Citation Index Expanded, the Social Sciences Citation Index және the Arts & Humanities Citation Index-ке қабылдау мәселесін қарастыруда. Web of Science зерттеушілер, авторлар, баспашылар мен мекемелерге контент тереңдігі мен сапасын ұсынады. ҚР ҰҒА Хабарлары. Геология және техникалық ғылымдар сериясы Emerging Sources Citation Index-ке енуі біздің қоғамдастық үшін ең өзекті және беделді геология және техникалық ғылымдар бойынша контентке адалдығымызды білдіреді.*

*НАН РК сообщает, что научный журнал «Известия НАН РК. Серия геологии и технических наук» был принят для индексирования в Emerging Sources Citation Index, обновленной версии Web of Science. Содержание в этом индексировании находится в стадии рассмотрения компанией Clarivate Analytics для дальнейшего принятия журнала в the Science Citation Index Expanded, the Social Sciences Citation Index и the Arts & Humanities Citation Index. Web of Science предлагает качество и глубину контента для исследователей, авторов, издателей и учреждений. Включение Известия НАН РК. Серия геологии и технических наук в Emerging Sources Citation Index демонстрирует нашу приверженность к наиболее актуальному и влиятельному контенту по геологии и техническим наукам для нашего сообщества.*

Б а с р е д а к т о р ы

э. ғ. д., профессор, ҚР ҰҒА академигі

**И.К. Бейсембетов**

Бас редакторының орынбасары

**Жолтаев Г.Ж.** проф., геол.-мин. ғ. докторы

Р е д а к ц и я а л қ а с ы:

**Абаканов Т.Д.** проф. (Қазақстан)  
**Абишева З.С.** проф., академик (Қазақстан)  
**Агабеков В.Е.** академик (Беларусь)  
**Алиев Т.** проф., академик (Әзірбайжан)  
**Бакиров А.Б.** проф., (Қырғыстан)  
**Беспәев Х.А.** проф. (Қазақстан)  
**Бишимбаев В.К.** проф., академик (Қазақстан)  
**Буктуков Н.С.** проф., академик (Қазақстан)  
**Булат А.Ф.** проф., академик (Украина)  
**Ганиев И.Н.** проф., академик (Тәжікстан)  
**Грэвис Р.М.** проф. (АҚШ)  
**Ерғалиев Г.К.** проф., академик (Қазақстан)  
**Жуков Н.М.** проф. (Қазақстан)  
**Кенжалиев Б.К.** проф. (Қазақстан)  
**Қожахметов С.М.** проф., академик (Қазақстан)  
**Конторович А.Э.** проф., академик (Ресей)  
**Курскеев А.К.** проф., академик (Қазақстан)  
**Курчавов А.М.** проф., (Ресей)  
**Медеу А.Р.** проф., академик (Қазақстан)  
**Мұхамеджанов М.А.** проф., корр.-мүшесі (Қазақстан)  
**Нигматова С.А.** проф. (Қазақстан)  
**Оздоев С.М.** проф., академик (Қазақстан)  
**Постолатий В.** проф., академик (Молдова)  
**Ракишев Б.Р.** проф., академик (Қазақстан)  
**Сейтов Н.С.** проф., корр.-мүшесі (Қазақстан)  
**Сейтмуратова Э.Ю.** проф., корр.-мүшесі (Қазақстан)  
**Степанец В.Г.** проф., (Германия)  
**Хамфери Дж.Д.** проф. (АҚШ)  
**Штейнер М.** проф. (Германия)

«ҚР ҰҒА Хабарлары. Геология мен техникалық ғылымдар сериясы».

**ISSN 2518-170X (Online),**

**ISSN 2224-5278 (Print)**

Меншіктенуші: «Қазақстан Республикасының Ұлттық ғылым академиясы» РҚБ (Алматы қ.).

Қазақстан республикасының Мәдениет пен ақпарат министрлігінің Ақпарат және мұрағат комитетінде 30.04.2010 ж. берілген №10892-Ж мерзімдік басылым тіркеуіне қойылу туралы куәлік.

Мерзімділігі: жылына 6 рет.

Тиражы: 300 дана.

Редакцияның мекенжайы: 050010, Алматы қ., Шевченко көш., 28, 219 бөл., 220, тел.: 272-13-19, 272-13-18,  
<http://nauka-nanrk.kz/geology-technical.kz>

---

© Қазақстан Республикасының Ұлттық ғылым академиясы, 2018

Редакцияның Қазақстан, 050010, Алматы қ., Қабанбай батыра көш., 69а.

мекенжайы: Қ. И. Сәтбаев атындағы геология ғылымдар институты, 334 бөлме. Тел.: 291-59-38.

Типографияның мекенжайы: «Аруна» ЖК, Алматы қ., Муратбаева көш., 75.

Г л а в н ы й р е д а к т о р  
д. э. н., профессор, академик НАН РК

**И. К. Бейсембетов**

Заместитель главного редактора

**Жолтаев Г.Ж.** проф., доктор геол.-мин. наук

Р е д а к ц и о н н а я к о л л е г и я:

**Абаканов Т.Д.** проф. (Казахстан)  
**Абишева З.С.** проф., академик (Казахстан)  
**Агабеков В.Е.** академик (Беларусь)  
**Алиев Т.** проф., академик (Азербайджан)  
**Бакиров А.Б.** проф., (Кыргызстан)  
**Беспаяев Х.А.** проф. (Казахстан)  
**Бишимбаев В.К.** проф., академик (Казахстан)  
**Буктуков Н.С.** проф., академик (Казахстан)  
**Булат А.Ф.** проф., академик (Украина)  
**Ганиев И.Н.** проф., академик (Таджикистан)  
**Грэвис Р.М.** проф. (США)  
**Ергалиев Г.К.** проф., академик (Казахстан)  
**Жуков Н.М.** проф. (Казахстан)  
**Кенжалиев Б.К.** проф. (Казахстан)  
**Кожамметов С.М.** проф., академик (Казахстан)  
**Конторович А.Э.** проф., академик (Россия)  
**Курскеев А.К.** проф., академик (Казахстан)  
**Курчавов А.М.** проф., (Россия)  
**Медеу А.Р.** проф., академик (Казахстан)  
**Мухамеджанов М.А.** проф., чл.-корр. (Казахстан)  
**Нигматова С.А.** проф. (Казахстан)  
**Оздоев С.М.** проф., академик (Казахстан)  
**Постолатий В.** проф., академик (Молдова)  
**Ракишев Б.Р.** проф., академик (Казахстан)  
**Сейтов Н.С.** проф., чл.-корр. (Казахстан)  
**Сейтмуратова Э.Ю.** проф., чл.-корр. (Казахстан)  
**Степанец В.Г.** проф., (Германия)  
**Хамфери Дж.Д.** проф. (США)  
**Штейнер М.** проф. (Германия)

«Известия НАН РК. Серия геологии и технических наук».

**ISSN 2518-170X (Online),**

**ISSN 2224-5278 (Print)**

Собственник: Республиканское общественное объединение «Национальная академия наук Республики Казахстан (г. Алматы)

Свидетельство о постановке на учет периодического печатного издания в Комитете информации и архивов Министерства культуры и информации Республики Казахстан №10892-Ж, выданное 30.04.2010 г.

Периодичность: 6 раз в год

Тираж: 300 экземпляров

Адрес редакции: 050010, г. Алматы, ул. Шевченко, 28, ком. 219, 220, тел.: 272-13-19, 272-13-18,  
<http://nauka-nanrk.kz/geology-technical.kz>

---

© Национальная академия наук Республики Казахстан, 2018

Адрес редакции: Казахстан, 050010, г. Алматы, ул. Кабанбай батыра, 69а.

Институт геологических наук им. К. И. Сатпаева, комната 334. Тел.: 291-59-38.

Адрес типографии: ИП «Аруна», г. Алматы, ул. Муратбаева, 75

E d i t o r i n c h i e f

doctor of Economics, professor, academician of NAS RK

**I. K. Beisembetov**

Deputy editor in chief

**Zholtayev G.Zh.** prof., dr. geol-min. sc.

E d i t o r i a l b o a r d:

**Abakanov T.D.** prof. (Kazakhstan)  
**Abisheva Z.S.** prof., academician (Kazakhstan)  
**Agabekov V.Ye.** academician (Belarus)  
**Aliyev T.** prof., academician (Azerbaijan)  
**Bakirov A.B.** prof., (Kyrgyzstan)  
**Bespayev Kh.A.** prof. (Kazakhstan)  
**Bishimbayev V.K.** prof., academician (Kazakhstan)  
**Buktukov N.S.** prof., academician (Kazakhstan)  
**Bulat A.F.** prof., academician (Ukraine)  
**Ganiyev I.N.** prof., academician (Tadjikistan)  
**Gravis R.M.** prof. (USA)  
**Yergaliev G.K.** prof., academician (Kazakhstan)  
**Zhukov N.M.** prof. (Kazakhstan)  
**Kenzhaliyev B.K.** prof. (Kazakhstan)  
**Kozhakhmetov S.M.** prof., academician (Kazakhstan)  
**Kontorovich A.Ye.** prof., academician (Russia)  
**Kurskeyev A.K.** prof., academician (Kazakhstan)  
**Kurchavov A.M.** prof., (Russia)  
**Medeu A.R.** prof., academician (Kazakhstan)  
**Muhamedzhanov M.A.** prof., corr. member. (Kazakhstan)  
**Nigmatova S.A.** prof. (Kazakhstan)  
**Ozdoev S.M.** prof., academician (Kazakhstan)  
**Postolatii V.** prof., academician (Moldova)  
**Rakishev B.R.** prof., academician (Kazakhstan)  
**Seitov N.S.** prof., corr. member. (Kazakhstan)  
**Seitmuratova Ye.U.** prof., corr. member. (Kazakhstan)  
**Stepanets V.G.** prof., (Germany)  
**Humphery G.D.** prof. (USA)  
**Steiner M.** prof. (Germany)

**News of the National Academy of Sciences of the Republic of Kazakhstan. Series of geology and technology sciences.**

**ISSN 2518-170X (Online),**

**ISSN 2224-5278 (Print)**

Owner: RPA "National Academy of Sciences of the Republic of Kazakhstan" (Almaty)

The certificate of registration of a periodic printed publication in the Committee of information and archives of the Ministry of culture and information of the Republic of Kazakhstan N 10892-Ж, issued 30.04.2010

Periodicity: 6 times a year

Circulation: 300 copies

Editorial address: 28, Shevchenko str., of. 219, 220, Almaty, 050010, tel. 272-13-19, 272-13-18,  
<http://nauka-nanrk.kz/geology-technical.kz>

---

© National Academy of Sciences of the Republic of Kazakhstan, 2018

Editorial address: Institute of Geological Sciences named after K.I. Satpayev  
69a, Kabanbai batyr str., of. 334, Almaty, 050010, Kazakhstan, tel.: 291-59-38.

Address of printing house: ST "Aruna", 75, Muratbayev str, Almaty

**NEWS**

OF THE NATIONAL ACADEMY OF SCIENCES OF THE REPUBLIC OF KAZAKHSTAN

**SERIES OF GEOLOGY AND TECHNICAL SCIENCES**

ISSN 2224-5278

<https://doi.org/10.32014/2018.2518-170X.41>

Volume 5, Number 431 (2018), 110 – 119

ISRSTI 30.15.27

UDC 534.014

**K. A. Kabyzbekov, A. D. Dasibekov, Kh. K. Abdrakhmanova,  
P. A. Saidakhmetov, E. B. Issayev, B. A. Urmashiev**

M. Auezov South Kazakhstan state University (SKSU), Shymkent, Kazakhstan.

E-mail: kenkab@mail.ru, dasibekjv.azhibek@mail.ru, khadi\_kab@mail.ru, timpf\_ukgu@mail.ru,  
erzhanisaev@mail.ru, bagdaulet-urmachantegi@mail.ru

**CALCULATION AND VISUALIZATION  
OF OSCILLATING SYSTEMS**

**Abstract.** The article presents the calculation and visualization of natural, damping and forced oscillations of a harmonic oscillator. The input parameters are the natural frequency, the initial coordinates and velocities of the system, the frequency of the driving force and its amplitude. The program is worked out and calculations and visualization of the oscillating system are carried out using the MatLab language: there are the graphs of the coordinates and system velocities versus time for natural, damping and forced oscillations of the harmonic oscillator. For damping oscillations such graphs are drawn at various magnitudes of the damping coefficients. The system of differential equations is solved by using the ode45 procedure. The program allows carrying out the experiments at different values of the input parameters. It is shown that the coordinate and velocity amplitudes of the damping harmonic oscillations exponentially decrease with time and asymptotically approach zero. This happens because the friction force work dissipates the oscillator energy. In a forced oscillation the system oscillates with the frequency of the driving force. There are assignments for student's self study. The results of calculation and visualization of the oscillating systems are used in the theoretical mechanics.

**Key words:** harmonic oscillator, natural, damped and forced oscillations, damping coefficient, natural frequency, driving force.

**Introduction.** Nowadays all educational institutions of Kazakhstan are provided with computer hardware and software, interactive boards and internet. Almost all teachers have completed language and computer courses for professional development. Hence the educational institutions have all conditions for using computer training programs and models for performing computer laboratory works. During several years we have been conducting the work on organization computer laboratory works on physics with use of resources of the Fizikon Company [1, 2] which are developed at Al-Farabi Kazakh National University by V.V.Kashkarov and his group. Some of worksheet templates for computer laboratory works are introduced in educational process of our university and schools of the Southern Kazakhstan [3-31]. Students of the physics specialties 5B060400 and 5B011000 successfully master the discipline "Computer modeling of physical phenomena" which is the logical continuation of the disciplines "Information technologies in teaching physics" and "Use of electronic textbooks in teaching physics". The aim of this discipline is to study and learn the MATLAB program language [32] system, acquaintance with its huge opportunities for modeling and visualization of physical processes. The present article is devoted to calculation and visualization of natural, damping and forced oscillations of a harmonic oscillator by using the package of MATLAB applied programs.

Formulation of the problem. **The natural oscillations of a harmonic oscillator (spring-mass system)** is described by differential equation of the second order:

$$\ddot{x} + \omega^2 x = 0$$

where  $\omega^2 = \frac{k}{m}$ , and  $k$  is the rigidity of the spring,  $m$  is the mass of the oscillator.

For solving this equation we transform it into two differential equations of the first order and then use the ode45 procedure.

$$\frac{dv_x}{dt} + \omega^2 x = 0, \quad \frac{dx}{dt} = v_x$$

Let us to introduce new denotations  $z(1)=x$ ;  $z(2)=dx/dt$  and then write the initial equation in the form of system of differential equations of the first order. Solution of these equations requires creation of m-file under the name Oscillator.m.

The listing of m-file

```
function dy=Oscillator(t,z);
global w; %input the natural frequency of a harmonic oscillator
dy=zeros(2,1); % input the column-vector with dimension 2 x 1
dy(1)=z(2); % input the equivalent differential equation
dy(2)=-w^2*z(1); % input the equivalent differential equation
end
```

The parameters of the oscillator are introduced in the command line in the form of comments.

In the command line we write

```
>> global w; % cyclic frequency
>> k=9; % rigidity coefficient
>> m=1; % the oscillator mass
>> T=2*pi*sqrt(k/m); % calculation of the oscillation period
>> w=2*pi/T; % calculation of the natural cyclic frequency
>> r0=[0.5 1]; % the initial conditions
>> [t,Z]=ode45('Oscillator',[0:5*T/5000:5*T],r0); % solution of the system of % ordinary differential
equations (ODE)
>> figure(1); plot(t,Z(:,1)); % visualization of the dependence x=x(t)
>> grid on % drawing the coordinate grid
```

The result is presented in the figure 1.

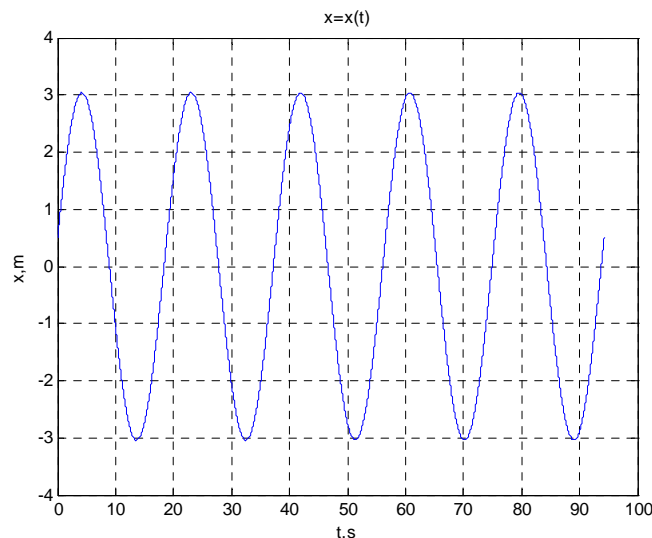


Figure 1 – The graph of the harmonic oscillator coordinate versus time

```
>> figure(2); plot(t,Z(:,2)); % visualization of the dependence v=v(t)
```

```
>> grid on % drawing the coordinate grid
```

The result is presented in the figure 2.

```
>> figure(3); plot(Z(:,1),Z(:,2)); % visualization of the trajectory in the phase plane
```

```
>> grid on % drawing the coordinate grid
```

The result is presented in the figure 3.

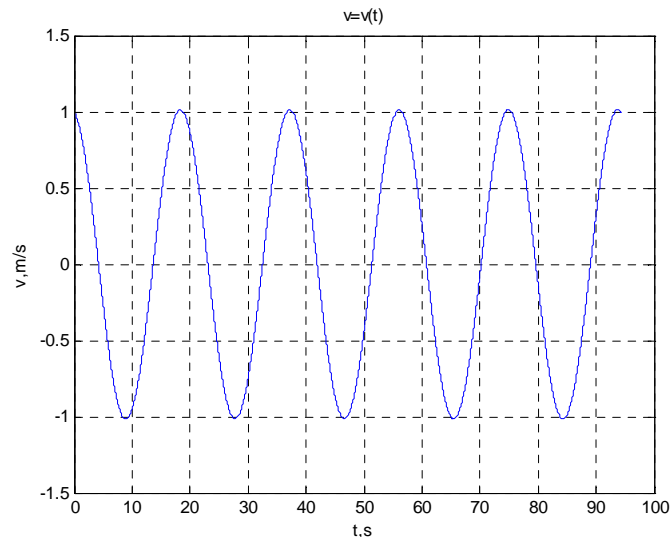


Figure 2 – The graph of the harmonic oscillator velocity versus time

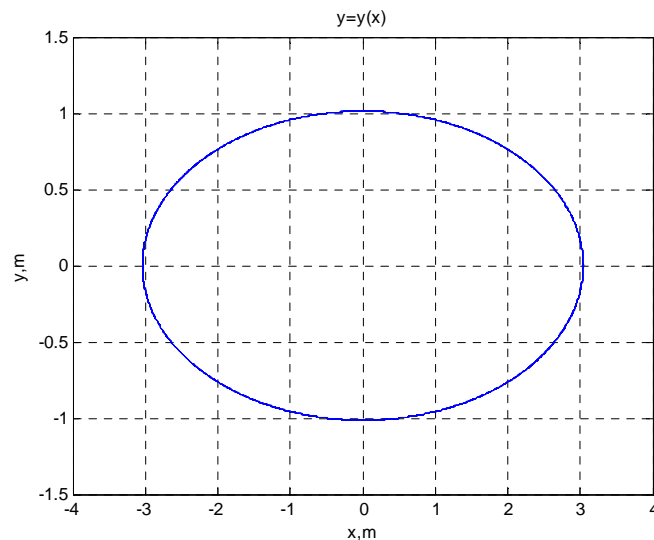


Figure 3 – Phase trajectory of the harmonic oscillator

**The damping oscillations of the harmonic oscillator** occur at the action of two forces: the restoring force  $f = -kx$  and the friction force  $f_l = -cdx/dt$ . Hence the equation of the damping oscillation is

$$m \frac{d^2x}{dt^2} + c \frac{dx}{dt} + kx = 0$$

It is necessary to solve this equation for the given mass and rigidity coefficient.

$$\frac{d^2x}{dt^2} = -\beta \frac{dx}{dt} - \omega^2 x$$

where  $\beta = \frac{c}{m}$ ,  $\omega^2 = \frac{k}{m}$ . For solving this equation we transform it into two differential equations of the first order and then use the ode45 procedure.

$$\frac{dv_x}{dt} = -\beta v_x - \omega^2 x; \quad v_x = \frac{dx}{dt}$$

At first, we introduce new denotations  $y(1) = x$ ;  $y(2) = dx/dt$  and then write the initial equation in the form of system of differential equations of the first order:



$$\frac{dy_1}{dt} = y_2, \quad \frac{dy_2}{dt} = -\omega^2 y_1 - \beta y_2$$

Then we create the m-file of the function `oscil` describing the right sides of this system of equations.

The listing of the m-file of the function `oscil`

```
function dydt=oscil(t,y)
```

```
global w2 b; % input the global variables
```

```
dydt=[y(2); -w2*y(1)-b*y(2)];
```

Let us find the solution of the system of equations using the `ode45` procedure and draw the graphs

In the command line we write

```
>> global w2 b; % input the global variables
```

```
>> w2=4; b=0.25; % input the parameters of the oscillator
```

```
>> x=2; %the initial coordinate
```

```
>> vx0=0; % the initial velocity
```

```
>> [t,y]=ode45(@oscil,[0 30],[2;0]); % solution of the ODE
```

```
>> plot(t, y(:, 1), '-', t, y(:, 2), '--') % drawing the graphs of the coordinate and % velocity versus time
```

```
>> grid on % drawing the coordinate grid
```

```
>> xlabel('time t'); % input the title of the x axis
```

```
>> ylabel('solution x'); % input the title of the y axis
```

```
>> legend('coordinate','velocity'); % input the legend of coordinate and velocity
```

```
>> title('Solution of oscillations equation '); % input the title of the graph
```

The result is presented in the figure 4

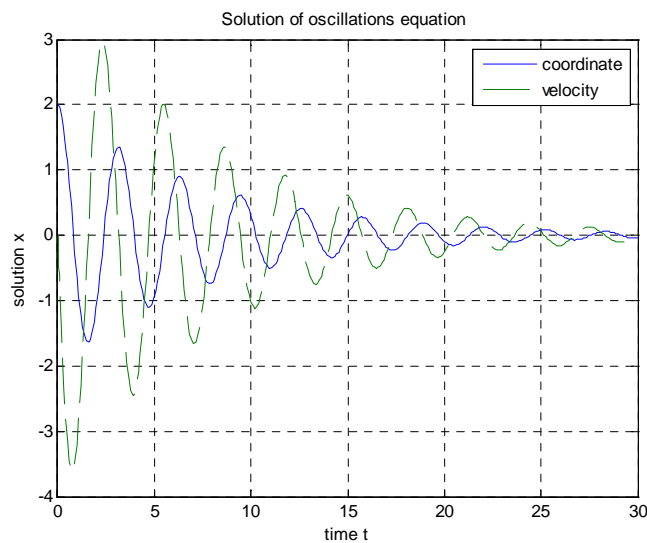


Figure 4 – The dependence of the velocity and coordinate of the harmonic oscillator upon the time

```
>> % The damping coefficient b=0.5
```

```
>> w2=4; b=0.5; % input the oscillator parameters
```

```
>> x=2; %the initial coordinate
```

```
>> vx0=0; % the initial velocity
```

```
>> [t,y]=ode45(@oscil,[0 30],[2;0]); % solution of the ODE
```

```
>> plot(t, y(:, 1), '-', t, y(:, 2), '--') % drawing the graphs of the coordinate and %velocity versus time
```

```
>> grid on % drawing the coordinate grid
```

```
>> xlabel('time t'); % input the title of the x axis
```

```
>> ylabel('solution x'); % input the title of the y axis
```

```
>> legend('coordinate','velocity'); % input the legend of coordinate and velocity
```

```
>> title('Solution of oscillations equation '); % input the title of the graph
```

The result is presented in the figure 5

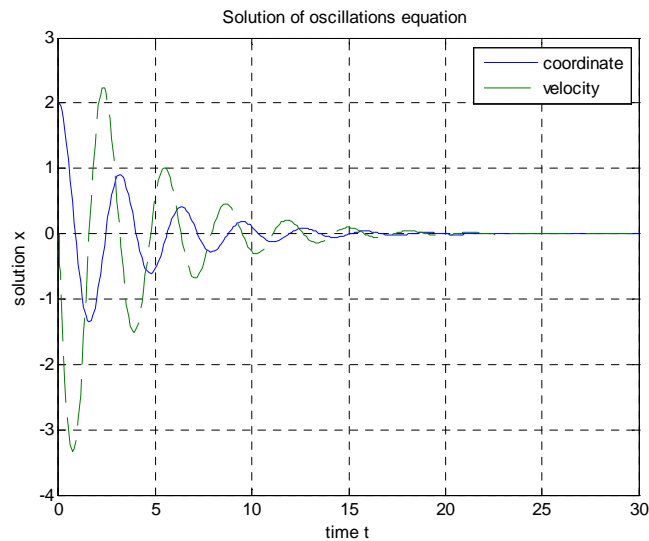


Figure 5 – The dependence of the velocity and coordinate of the harmonic oscillator upon the time at  $b = 0.5$

**The forced oscillations of a harmonic oscillator** occur under the action of a driving force  $F(t)$ . Let the driving force be a periodical one obeying the law

$$F(t) = F_0 \cos(\omega t)$$

where  $F_0 = \text{const}$  is the amplitude of the driving force,  $\omega$  is the cyclic frequency.

$$\frac{d^2 x}{dt^2} = -\beta \frac{dx}{dt} - \omega^2 x + \frac{F_0}{m} \cos(\omega_d t)$$

where  $\beta = \frac{c}{m}$ ,  $\omega^2 = \frac{k}{m}$  is the square of the natural frequency of the harmonic oscillator,  $\omega_d$  is the cyclic frequency of the driving force and  $f = \frac{F_0}{m}$ . Let us write the initial differential equation of the second order in the form of two differential equations of the first order:

$$\frac{dv_x}{dt} = -\beta v_x - \omega^2 x + \frac{F_0}{m} \cos(\omega_d t); \quad v_x = \frac{dx}{dt}$$

Introducing the denotations  $y_1 = x$ ,  $y_2 = dx/dt$  we rewrite the above given two differential equations of the first order as the followings

$$\frac{dy_1}{dt} = y_2, \quad \frac{dy_2}{dt} = -\omega^2 y_1 - \beta y_2 + f \cdot \cos(\omega_d t)$$

Then create the m-file function `oscilb` describing the right sides of this system of equations.

The listing of m-file of the function `oscilb`

function `dydt=oscilb(t,y)`

global `w b wd f`; % input the global variable

`dydt=[y(2); -w*y(1)-b*y(2)+ f *cos(wd * t)];`

We find the solution of the system of equations using the `ode45` procedure and draw the graph.

In the command line we write:

`>> global w b wb f; % input the global variable`

`>> w=4; b=0.5; wd=6; f=4;`

`>> x=2; vx0=0;`

```
>> [t,y]=ode45(@oscilb,[0 30],[2;0]);
>> plot(t,y(:,1),'- ',t,y(:, 2),'- ');
>> grid on
```

The result is presented in the figure 6

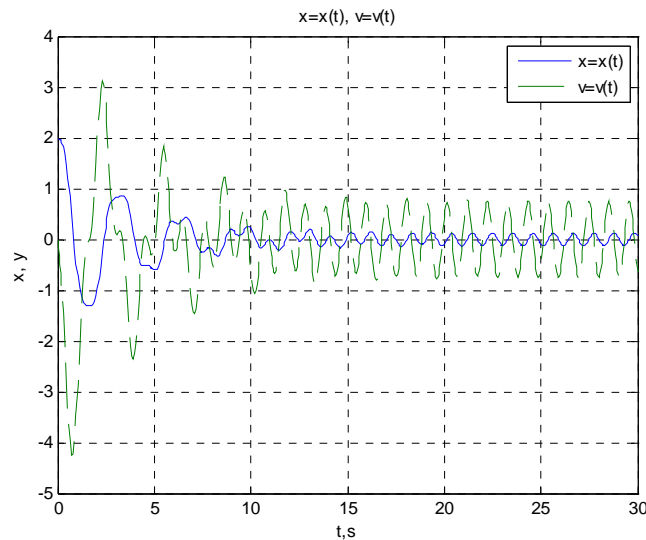


Figure 6 – The dependence of the velocity and coordinate of the harmonic oscillator upon the time at  $w = 4$ ,  $b = 0.5$ ,  $w_d = 6$ ,  $f = 4$

```
>> plot(t,y(:,1))
>> grid on
```

The result is presented in the figure 7

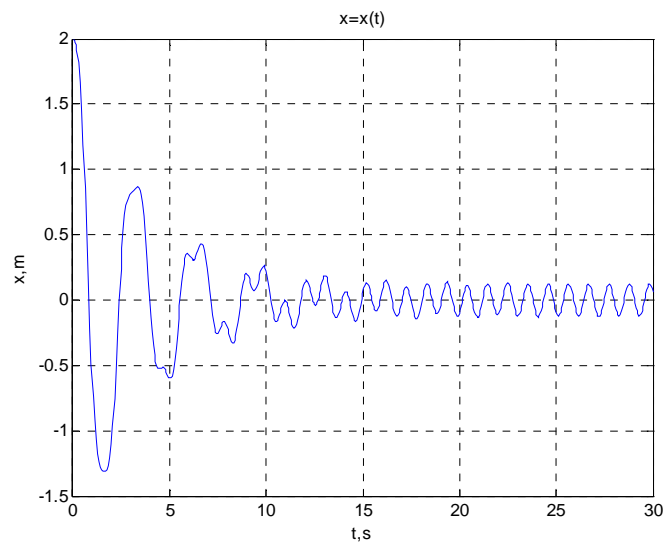


Figure 7 – The graph of the coordinate versus time during the forced oscillation at  $w = 4$ ,  $b = 0.5$ ,  $w_d = 6$ ,  $f = 4$

```
>> plot(t,y(:,2))
>> grid on
```

The result is presented in the figure 8

The figures 4 and 5 show that the amplitudes of the coordinate and velocity of the harmonic oscillator in its damping oscillation exponentially decrease with time and asymptotically approach zero.

This is because the friction force work dissipates the energy of the oscillator.

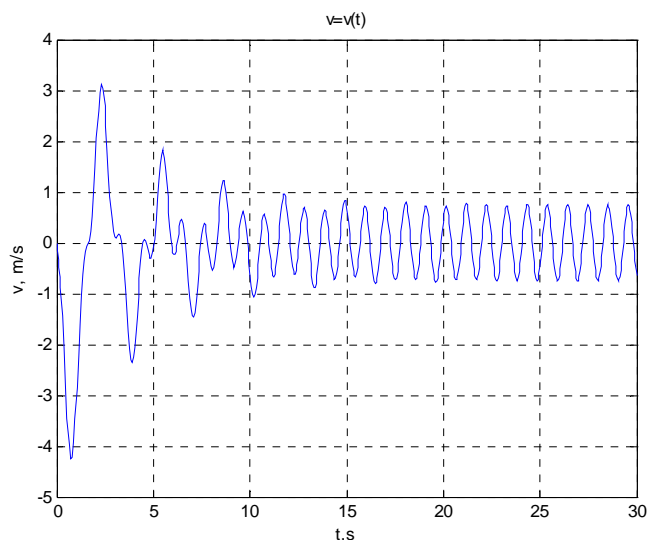


Figure 8 – The graph of the velocity of forced oscillations versus time at  $w = 4$ ,  $b = 0.5$ ,  $w_d = 6$ ,  $f = 4$

The figures 7 and 8 present that at the action of a driving force the oscillation amplitude after a certain time stops decreasing and becomes constant because the oscillation occurs at the frequency of the driving force.

**Conclusion.** The article presents the calculation and visualization of natural, damping and forced oscillations of a harmonic oscillator. The input parameters are the natural frequency, the initial coordinates and velocities of the system, the frequency of the driving force and its amplitude. The program is worked out and calculations and visualization of the oscillating system are carried out using the MatLab language: there are the graphs of the coordinates and system velocities versus time for natural, damping and forced oscillations of the harmonic oscillator. For damping oscillations such graphs are drawn at various magnitudes of the damping coefficients. The system of differential equations is solved by using the ode45 procedure. The program allows carrying out the experiments at different values of the input parameters. There are assignments for student's self study. The results of calculation and visualization of the oscillating systems are used in the theoretical mechanics.

#### REFERENCES

- [1] CD of the open JSC "Phizicon". «The open physics 1.1». 2001.
- [2] <http://elektronika.newmail.ru>
- [3] Kabyzbekov K.A., Abdrakhmanova Kh.K., Abekova Zh.A., Abdraimov R.T., Ualikhanova B.S. Calculation and visualization of a system- an electron in a deep square potential well, with use of the software package of MATLAB // Proceeding of the III International Scientific and Practical Conference «Topical researches of the World Science». (June 28, 2017, Dubai, UAE). July 2017. Vol. 1, N 23. P. 7-13.
- [4] Kabyzbekov K., Saidullaeva N., Spabekova R., Omashova G, Tagaev N., Bitemirova A., Berdieva M. Model of a blank form for computer laboratory work on research of the speed selector // Journal of Theoretical and Applied Information Technology. 15th July 2017. Vol. 95, N 13. P. 2999-3009. JATIT & LLS. Indexada en Scopus.
- [5] Kabyzbekov K., Omashova G, Spabekova R, Saidullaeva N, Saidakhmetov P. Junusbtikova S Management and organization of computer laboratory work in physics education // Espacios. Año 2017. Vol. 38, N 45. P. 35. Indexada en Scopus, Google Scholar.
- [6] Kabyzbekov K.A., Saidakhmetov P. A, Arysbaeva A.S. Worksheet template for organization the independent performance of computer laboratory works // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. 2013. N 6. P. 82-89.
- [7] Kabyzbekov K.A., Saidakhmetov P. A, Baidullaeva L.E., Abduraimov R. A technique of use of computer models for photo-effect and Compton effect studying, worksheet template for organization the performance of computer laboratory works // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. 2013. N 6. P. 114-121.

- [8] Kabyzbekov K.A., Saidahmetov P. A. Turganova T.K, Nurullaev M. A, Baidullaeva L.E. Model of a lesson on converging and diverging lenses // Proceedings of NAN RK. Series physical-mat. 2014. N 2. P. 286-294.
- [9] Kabyzbekov K.A., Ashirbaev H. A, Saidahmetov P. A, Rustemova K.Zh., Baidullaeva L. E. Worksheet template for organization the performance of computer laboratory work on study the diffraction of light // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan, Series of Physics and Mathematics. 2015. N 1(299). P. 71-77.
- [10] Kabyzbekov K.A., Ashirbaev H. A, Takibaeva G.A, Saparbaeva E. M, Baidullaeva L. E, Adineeva SH.I. Worksheet template for organization the performance of computer laboratory work on study the motion of charged particles in a magnetic field // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. 2015. N 1(299). P. 80-87.
- [11] Kabyzbekov K.A., Ashirbaev . H A, Saidakhmetov, P A, Baigulova Z.A., Baidullaeva L.E. Worksheet template for organization the performance of computer laboratory work on study the Newton's rings // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. 2015. N 1(299). P. 14-20.
- [12] Kabyzbekov K.A., Ashirbaev H.A., Sabalakhova A.P., Dzhumagalieva A.I. Worksheet template for organization the performance of computer laboratory work on study the phenomenon of light interference // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. 2015. N 3(301). P. 131-136.
- [13] Kabyzbekov K.A., Ashirbaev H.A., Sabalakhova A.P., Dzhumagalieva A.I. Worksheet template for organization the performance of computer laboratory work on study the Doppler-effect // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. 2015. N 3(301). P. 155-160.
- [14] Kabyzbekov K.A., Ashirbaev H.A., Arysbaeva A.S., Dzhumagalieva A.I. Worksheet template for organization the performance of computer laboratory work on study physical phenomena // Modern high technologies. M., 2015. N 4. P. 40-43.
- [15] Kabyzbekov K. A., Saidakhmetov P. A., Ashirbaev Kh. A., Omashova G. Sh., Berdalieva J. Worksheet template for organization the performance of computer laboratory work on study electromagnetic oscillations // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics And Mathematics. 2016. N 1(305). P. 111-116.
- [16] Kabyzbekov K.A., Saidakhmetov P.A., Omashova G.Sh., Berdalieva J., Dzhumagalieva A.I. Worksheet template for organization the performance of computer laboratory work on study the interaction between two infinitely long parallel current-carrying conductors // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. 2016. N 1(305). P. 135-140.
- [17] Kabyzbekov K.A., Saidakhmetov P.A., Omashova G.Sh., Suttibaeva D.I., Kozybakova G.N. Worksheet template for organization the performance of computer laboratory work on study isobaric process // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. 2016. N 2. P. 92-97.
- [18] Kabyzbekov K.A., Omashova G.Sh., Saidakhmetov P.A., Nurullaev M.A., Artygalin N.A. Worksheet template for organization the performance of computer laboratory work on study the Carnot cycle // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. 2016. N 2. P. 98-103.
- [19] Kabyzbekov K.A., Saidakhmetov P.A., Ashirbaev H.A., Abdubaeva Ph.I., Doskanova A.E. Study of the work done by gas on computer model // The Herald of NAN PK. 2016. N 2. P. 83-88.
- [20] Kabyzbekov K.A., Saidakhmetov P.A., Omashova G.Sh., Serikbaeva G.S., Suyerkulova Zh.N. Worksheet template for organization the performance of computer laboratory work on study simple harmonic motions // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. 2016. N 2. P. 84-91.
- [21] Kabyzbekov K.A., Madjarov N.T., Saidakhmetov P.A. An Independent design of research assignments for computer laboratory work on thermodynamics // Proceedings of the IX International scientific-methodical conference "Teaching natural Sciences (biology, physics, chemistry), mathematics and computer science". Tomsk, 2016. P. 93-99.
- [22] Kabyzbekov K.A., Saidakhmetov P.A., Omashova G.Sh. Organization of computer laboratory work on study the inductor reactance in an ac circuit // Proceedings of NAN RK. 2017. N 1. P. 77-82.
- [23] Kabyzbekov K.A., Saidakhmetov P.A., Omashova G.Sh., Ashirbaev H.A., Abekova J.A. Organization of computer laboratory works on study of the isotherms of a real gas. Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. 2017. N 1. P. 77-83.
- [24] Kabyzbekov K.A., Saidakhmetov P.A., Omashova G.Sh. Organization of computer laboratory works on study of the phenomenon of beats // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. 2017. N 2. P. 104-110.
- [25] Kabyzbekov K.A., Omashova G.Sh., Spabekova R.S., Saidakhmetov P.A., Serikbaeva G., Arysbaeva A.S. Worksheet template for organization the performance of computer laboratory work on study the isothermal process // Herald of the National Academy of Sciences of Kazakhstan. 2017. N 3. P. 19-207.
- [26] Kabyzbekov K.A., Omashova G.Sh., Spabekova R.S., Saidakhmetov P.A., Abdrakhmanova Kh.K., Arysbaeva A.S. Independent design of assignment for performance of a computer lab on study isochoric process // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. 2017. N 3. P. 127-134.

[27] Kabyzbekov K.A., Omashova G.Sh., Spabekova R.S., Saidakhmetov P.A., Serikbaeva G.S., Aktureeva G. Organization of computer laboratory works on study the turn-on and turn-off current of the power supply by using MATLAB software package // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. 2017. N 3. P. 139-146.

[28] Kabyzbekov K.A., Omashova G.Sh., Spabekova R.S., Saidakhmetov P.A., Serikbaeva G.S., Aktureeva G. Organization of computer labs for the study the velocity and height distribution of molecules from the Earth's surface by using MATLAB software package // Herald of RK NAS. 2017. N 3. P. 111-119.

[29] Kabyzbekov K.A., Ashirbayev H.A., Abdrakhmanova Kh.K., Dzhumagalieva A.I., Kydyrbekova J.B. Organization of laboratory work on study the electric and magnetic fields by using MATLAB software package // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. 2017. N 3(313). P. 206-212.

[30] Kabyzbekov K.A., Abdrakhmanova Kh.K., Omashova G.Sh., Kedelbaev B., Abekova J.A. Calculation and visualization of electric field of a space – charled sphere // News of the National Academy of Sciences of the Republic of Kazakhstan. Series of geology and technical sciences. 2018. Vol. 5, N 431. P. 201-209.

[31] Kabyzbekov K.A., Abdrakhmanova Kh.K., Saidakhmetov P.A., Sultanbek T.S., Kedelbaev B.Sh. Calculation and visualization of isotopes separation process using MATLAB program // News of the National Academy of Sciences of the Republic of Kazakhstan. Series of geology and technical sciences. 2018. Vol. 5, N 431. P. 218-225.

[32] Porsnev S.V. Computer simulation of physical processes in the package MATLAB. M.: Hot Line-Telecom, 2003. 592 p.

**К. А. Кабылбеков, А. Д. Дасибеков, Х. К. Абдрахманова,  
П. А. Саидахметов, Е. Б. Исаев, Б. А. Урмашев**

М. Әуезов атындағы Оңтүстік Қазақстан мемлекеттік, Шымкент, Қазақстан

#### **ТЕРБЕЛМЕЛІ ЖҮЙЕНІ ЕСЕПТЕУ ЖӘНЕ БЕЙНЕЛЕУ**

**Аннотация.** Гармоникалық осциллятордың еркін, өшпелі және мәжбүр тербелістерін есептеу мен бейнелеу ұсынылады. Осциллятордың параметрлері ретінде оның өзіндік жиілігі, бастапқы координаталары мен жылдамдығы, мәжбүрлеуші күштің жиілігі алынған. Тербелмелі жүйені Matlab программалық ортасында есептеу мен бейнелеу үшін программа құрылған: гармоникалық осциллятордың еркін, өшпелі және мәжбүр тербелістері есептеліп, оның координаталары мен қозғалу жылдамдығының уақытқа тәуелділік графиктері салынған. Өшпелі тербелі үшін өшу коэффициентінің әр түрлі мәндеріндегі графиктер салынған. Дифференциалдық тендулер жүйесін шешу үшін ode45 процедурасы қолданылды. Программа тербелмелі жүйенің параметрлерін өзгерте отырып эксперименттер жүргізуге мүмкіндік береді.

Есептеулер мен бейнелеулер нәтижесінде өшпелі тербелістің координаталар мен жылдамдық амплитудаларының уақыт өткен сайын экспоненциалды кемитіні көрсетілген, себебі үйкеліс күшінің жұмысы есебінен осциллятордың энергиясы шашырайды. Ал, мәжбүр тербелісте белгілі бір уақыттан соң тербеліс амплитудасы тұрақталатыны көрсетілген және қалған уақытта мәжбүрлеуші жиелікте тербеледі.

Өз бетінше жұмыс атқаруға арналған тапсырмалар берілген. Ұсынылған есептеулер мен бейнелеу нәтижелері теориялық механикада қолданылады.

**Түйін сөздер:** гармоникалық осциллятор, еркін, өшпелі және мәжбүр тербелістер, өшу коэффициенті, өзіндік, мәжбүрлеуші жиілік, сыртқы күш.

**К. А. Кабылбеков, А. Д. Дасибеков, Х. К. Абдрахманова,  
П. А. Саидахметов, Е. Б. Исаев, Б. А. Урмашев**

Южно-Казахстанский государственный университет им. М. Ауэзова, Шымкент, Казахстан

#### **РАСЧЕТ И ВИЗУАЛИЗАЦИЯ КОЛЕБАТЕЛЬНЫХ СИСТЕМ**

**Аннотация.** Предлагается расчет и визуализация свободного, затухающего и вынужденного колебаний гармонического осциллятора. Входными параметрами являются частота собственного колебания, начальные координаты и скорости системы, частота вынуждающей силы и ее амплитуда. Составлена программа и проведены расчеты и визуализация колебательной системы в среде Matlab: построены графики зависимости координат и скорости системы от времени при свободном, затухающем и вынужденном колебаниях гармо-

нического осциллятора. Для затухающего колебания построены такие графики для разных значений коэффициента затухания. При решении системы дифференциальных уравнений использована процедура ode45. Программа позволяет проводить эксперименты при различных значениях входных параметров. Показано, что амплитуда координаты и скорости затухающего гармонического осциллятора экспоненциально уменьшается со временем и асимптотически приближается к нулю. Это связано с рассеиванием энергии осциллятора за счет работы сил трения. При вынужденном колебании через определенное время колебание системы стабилизируется, что связано с тем что, после окончания затухания дальнейшее колебание происходит с частотой вынуждающей силы. Даны задания для самостоятельной работы. Результаты расчетов и визуализаций применяются в теоретической механике.

**Ключевые слова:** гармонический осциллятор, свободные, затухающие и вынужденные колебания, коэффициент затухания, собственная, частота, вынуждающая сила.

#### **Сведения об авторах:**

Кабылбеков К. А. – канд. физ.-мат. наук, доцент кафедры «Физика»

Дасибеков А. Д. – докт. техн. наук, профессор кафедры «Механика»

Абдрахманова Х. К. – канд. физ.-мат. наук, доцент кафедры «Физика»

Саидакхметов П. А. – канд. физ.-мат. наук, доцент кафедры «Физика»

Исаев Е. Б. – канд. техн. наук, зав. каф. «Биология»

Урмашев Б. – канд. техн. наук, доцент каф. «Химия»

#### **Information about authors:**

Kabyzbekov K. A. – M. Auezov South Kazakhstan state University (SKSU), Shymkent, Kazakhstan; kenkab@mail.ru; <https://orcid.org/0000-0001-8347-4153>

Dasibekov A. D. – M. Auezov South Kazakhstan state University (SKSU), Shymkent, Kazakhstan; dasibekjv.azhibek@mail.ru; <https://orcid.org/0000-0002-7148-5506>

Abdrakhmanova Kh. K. – M. Auezov South Kazakhstan state University (SKSU), Shymkent, Kazakhstan; khadi\_kab@mail.ru; <https://orcid.org/0000-0002-6110-970X>

Saidakhmetov P. A. – M. Auezov South Kazakhstan state University (SKSU), Shymkent, Kazakhstan; timpf\_ukgu@mail.ru; <https://orcid.org/0000-0002-9146-047X>

Issayev E. B. – M. Auezov South Kazakhstan state University (SKSU), Shymkent, Kazakhstan; erzhanisaev@mail.ru; <https://orcid.org/0000-0001-7536-5643>

Urmashhev B. A. – M. Auezov South Kazakhstan state University (SKSU), Shymkent, Kazakhstan; bagdaulet-urmachantegi@mail.ru; <https://orcid.org/0000-0001-6047-488X>

---

**Publication Ethics and Publication Malpractice  
in the journals of the National Academy of Sciences of the Republic of Kazakhstan**

For information on Ethics in publishing and Ethical guidelines for journal publication see <http://www.elsevier.com/publishingethics> and <http://www.elsevier.com/journal-authors/ethics>.

Submission of an article to the National Academy of Sciences of the Republic of Kazakhstan implies that the described work has not been published previously (except in the form of an abstract or as part of a published lecture or academic thesis or as an electronic preprint, see <http://www.elsevier.com/postingpolicy>), that it is not under consideration for publication elsewhere, that its publication is approved by all authors and tacitly or explicitly by the responsible authorities where the work was carried out, and that, if accepted, it will not be published elsewhere in the same form, in English or in any other language, including electronically without the written consent of the copyright-holder. In particular, translations into English of papers already published in another language are not accepted.

No other forms of scientific misconduct are allowed, such as plagiarism, falsification, fraudulent data, incorrect interpretation of other works, incorrect citations, etc. The National Academy of Sciences of the Republic of Kazakhstan follows the Code of Conduct of the Committee on Publication Ethics (COPE), and follows the COPE Flowcharts for Resolving Cases of Suspected Misconduct ([http://publicationethics.org/files/u2/New\\_Code.pdf](http://publicationethics.org/files/u2/New_Code.pdf)). To verify originality, your article may be checked by the Cross Check originality detection service <http://www.elsevier.com/editors/plagdetect>.

The authors are obliged to participate in peer review process and be ready to provide corrections, clarifications, retractions and apologies when needed. All authors of a paper should have significantly contributed to the research.

The reviewers should provide objective judgments and should point out relevant published works which are not yet cited. Reviewed articles should be treated confidentially. The reviewers will be chosen in such a way that there is no conflict of interests with respect to the research, the authors and/or the research funders.

The editors have complete responsibility and authority to reject or accept a paper, and they will only accept a paper when reasonably certain. They will preserve anonymity of reviewers and promote publication of corrections, clarifications, retractions and apologies when needed. The acceptance of a paper automatically implies the copyright transfer to the National Academy of Sciences of the Republic of Kazakhstan.

The Editorial Board of the National Academy of Sciences of the Republic of Kazakhstan will monitor and safeguard publishing ethics.

Правила оформления статьи для публикации в журнале смотреть на сайте:

[www.nauka-nanrk.kz](http://www.nauka-nanrk.kz)

**ISSN 2518-170X (Online), ISSN 2224-5278 (Print)**

<http://geolog-technical.kz/index.php/kz/>

Верстка Д. Н. Калкабековой

Подписано в печать 23.11.2018.

Формат 70x881/8. Бумага офсетная. Печать – ризограф.

14,7 п.л. Тираж 300. Заказ 6.