

ISSN 2518-170X (Online),  
ISSN 2224-5278 (Print)

ҚАЗАҚСТАН РЕСПУБЛИКАСЫ  
ҰЛТТЫҚ ҒЫЛЫМ АКАДЕМИЯСЫНЫҢ

# Х А Б А Р Л А Р Ы

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НАЦИОНАЛЬНОЙ АКАДЕМИИ НАУК  
РЕСПУБЛИКИ КАЗАХСТАН

## NEWS

OF THE ACADEMY OF SCIENCES  
OF THE REPUBLIC OF KAZAKHSTAN

ГЕОЛОГИЯ ЖӘНЕ ТЕХНИКАЛЫҚ ҒЫЛЫМДАР  
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СЕРИЯ  
ГЕОЛОГИИ И ТЕХНИЧЕСКИХ НАУК



SERIES  
OF GEOLOGY AND TECHNICAL SCIENCES

**6 (426)**

ҚАРАША – ЖЕЛТОҚСАН 2017 ж.  
НОЯБРЬ – ДЕКАБРЬ 2017 г.  
NOVEMBER – DECEMBER 2017

ЖУРНАЛ 1940 ЖЫЛДАН ШЫҒА БАСТАҒАН  
ЖУРНАЛ ИЗДАЕТСЯ С 1940 г.  
THE JOURNAL WAS FOUNDED IN 1940.

ЖЫЛЫНА 6 РЕТ ШЫҒАДЫ  
ВЫХОДИТ 6 РАЗ В ГОД  
PUBLISHED 6 TIMES A YEAR

АЛМАТЫ, ҚР ҰҒА  
АЛМАТЫ, НАН РК  
ALMATY, NAS RK

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«ҚР ҰҒА Хабарлары. Геология мен техникалық ғылымдар сериясы».

**ISSN 2518-170X (Online),**

**ISSN 2224-5278 (Print)**

Меншіктенуші: «Қазақстан Республикасының Ұлттық ғылым академиясы» РҚБ (Алматы қ.).

Қазақстан республикасының Мәдениет пен ақпарат министрлігінің Ақпарат және мұрағат комитетінде 30.04.2010 ж. берілген №10892-Ж мерзімдік басылым тіркеуіне қойылу туралы куәлік.

Мерзімділігі: жылына 6 рет.

Тиражы: 300 дана.

Редакцияның мекенжайы: 050010, Алматы қ., Шевченко көш., 28, 219 бөл., 220, тел.: 272-13-19, 272-13-18,  
<http://nauka-nanrk.kz/geology-technical.kz>

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Редакцияның Қазақстан, 050010, Алматы қ., Қабанбай батыра көш., 69а.

мекенжайы: Қ. И. Сәтбаев атындағы геология ғылымдар институты, 334 бөлме. Тел.: 291-59-38.

Типографияның мекенжайы: «Аруна» ЖК, Алматы қ., Муратбаева көш., 75.

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«Известия НАН РК. Серия геологии и технических наук».

**ISSN 2518-170X (Online),**

**ISSN 2224-5278 (Print)**

Собственник: Республиканское общественное объединение «Национальная академия наук Республики Казахстан (г. Алматы)

Свидетельство о постановке на учет периодического печатного издания в Комитете информации и архивов Министерства культуры и информации Республики Казахстан №10892-Ж, выданное 30.04.2010 г.

Периодичность: 6 раз в год

Тираж: 300 экземпляров

Адрес редакции: 050010, г. Алматы, ул. Шевченко, 28, ком. 219, 220, тел.: 272-13-19, 272-13-18,  
<http://nauka-nanrk.kz/geology-technical.kz>

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Институт геологических наук им. К. И. Сатпаева, комната 334. Тел.: 291-59-38.

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**News of the National Academy of Sciences of the Republic of Kazakhstan. Series of geology and technology sciences.**

**ISSN 2518-170X (Online),**

**ISSN 2224-5278 (Print)**

Owner: RPA "National Academy of Sciences of the Republic of Kazakhstan" (Almaty)

The certificate of registration of a periodic printed publication in the Committee of information and archives of the Ministry of culture and information of the Republic of Kazakhstan N 10892-Ж, issued 30.04.2010

Periodicity: 6 times a year

Circulation: 300 copies

Editorial address: 28, Shevchenko str., of. 219, 220, Almaty, 050010, tel. 272-13-19, 272-13-18,  
<http://nauka-nanrk.kz/geology-technical.kz>

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Editorial address: Institute of Geological Sciences named after K.I. Satpayev  
69a, Kabanbai batyr str., of. 334, Almaty, 050010, Kazakhstan, tel.: 291-59-38.

Address of printing house: ST "Aruna", 75, Muratbayev str, Almaty

## NEWS

OF THE NATIONAL ACADEMY OF SCIENCES OF THE REPUBLIC OF KAZAKHSTAN

SERIES OF GEOLOGY AND TECHNICAL SCIENCES

ISSN 2224-5278

Volume 6, Number 426 (2017), 255 – 263

UDC 539.3(043.3)

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**MATHEMATICAL THEORY OF VIBRATION OF ELASTIC  
OR VISCOELASTIC PLATES, UNDER NON-STATIONARY  
EXTERNAL INFLUENCES**

**Abstract.** In this work, attempt was made to present the mathematical theory of oscillations of an elastic or viscoelastic plate to study its dynamic behavior under nonstationary external influences. On the basis of this approach, exact equations of longitudinal and transverse oscillations of viscoelastic plates are derived with and without allowance for initial displacements and stresses, approximate equations for the physical nonlinearity of the material. For all problems, expressions are obtained for all displacements and stresses along the thickness of the plate and basic boundary-value formulated problems that lead to longitudinal or transverse vibrations of the plate. On the basis of exact equations some approximate equations that follow with some degree of accuracy are analyzed and approximate boundary value problems formulated for them.

**Key words:** elastic, viscoelastic, nonstationary, oscillations, nonlinear, deformable, longitudinal, transverse.

Investigation of wave processes in restricted deformable bodies are reduced to complicated mathematical problem, which is generally at the present stage can not be solved either analytical or numerical methods.

Even for deformable media which is described by the simplest models, such as elastic and viscoelastic media, many nonstationary problems have not been investigated and there are no methods to solve these problems in accurate formulation. Therefore, many applied problems in various fields of technology are solved on simplified models that reduce the spatial problems of dynamics to two-dimensional or one-dimensional ones. Such simplified models are plates, rods and shells.

All naturally occurring environments on the nature of the dynamic behavior can be divided into perfectly elastic and differential elastic.

The first group includes environments of mechanical characteristics that are close to each other. When studying dynamics and wave processes, such media can be considered as homogeneous medium with averaged mechanical characteristics.

Для дифференциально-упругих сред механические характеристики, составляющие двухкомпонентную среду, значительно различаются друг от друга.

For differential-elastic media, the mechanical characteristics which constituting the two-component medium differ significantly from each other.

We shall consider two-component media consisting of two elastic components or from an elastic porous skeleton and liquid filler.

We introduce the concept of the porosity of the medium.

The porosity of the medium will be denoted by a quantity determined by the formula:

$$K_0 = V_p / V_s, \quad (1)$$

where - the volume of the second component relative to the first medium in a volume element as a whole,  $V_s$  - the total volume of the elementary sample.

We'll assume, that  $K_0 = const$ .

The first type of two-component medium consisting of two elastic components is characterized by different conditions of adhesion between them and in the general case of the stress-strain relationship, we write in the form:

$$\begin{aligned}\sigma_{ij}^{(1)} &= \sigma_{ij}^{(1)} \left( \varepsilon_x^{(1)}, \varepsilon_y^{(1)}, \varepsilon_z^{(1)}; \varepsilon_x^{(2)}, \varepsilon_y^{(2)}, \varepsilon_z^{(2)}; \varepsilon_{xy}^{(1)}, \varepsilon_{yz}^{(1)}, \varepsilon_{xz}^{(1)}; \varepsilon_{xy}^{(2)}, \varepsilon_{yz}^{(2)}, \varepsilon_{xz}^{(2)} \right) \\ \sigma_{ij}^{(2)} &= \sigma_{ij}^{(2)} \left( \varepsilon_x^{(1)}, \varepsilon_y^{(1)}, \varepsilon_z^{(1)}; \varepsilon_x^{(2)}, \varepsilon_y^{(2)}, \varepsilon_z^{(2)}; \varepsilon_{xy}^{(1)}, \varepsilon_{yz}^{(1)}, \varepsilon_{xz}^{(1)}; \varepsilon_{xy}^{(2)}, \varepsilon_{yz}^{(2)}, \varepsilon_{xz}^{(2)} \right)\end{aligned}\quad (2)$$

where the index " 1 " refers to the first component, the index " 2 " - to the second.

The second type of two-component medium requires some explanation.

The term "pore" refers to a medium with openly communicating pores.

The connection between the constituent components of the medium will be considered imperfect, i.e. The liquid component can not flow out of the medium.

Let the continuous deformable medium consist of two elastic continua with different mechanical characteristics whose densities will be denoted by  $\rho_j (j = 1, 2)$ , the displacement vectors of the points.

$$\vec{U}^{(j)} \quad (j = 1, 2).$$

Depending on the deformation stresses are [1]

$$\begin{aligned}\sigma_{\alpha\alpha}^{(1)} &= -\alpha_2 + \lambda_1 e^{(1)} + 2\mu_1 \varepsilon_{\alpha\alpha}^{(1)} + \lambda_3 e^{(2)} + 2\mu_3 \varepsilon_{\alpha\alpha}^{(2)}; \\ \frac{1}{2} \left( \sigma_{\alpha\beta}^{(1)} + \sigma_{\beta\alpha}^{(1)} \right) &= 2\mu_1 \varepsilon_{\alpha\beta}^{(1)} + 2\mu_3 \varepsilon_{\alpha\beta}^{(2)}; \\ \frac{1}{2} \left( \sigma_{\alpha\beta}^{(1)} - \sigma_{\beta\alpha}^{(1)} \right) &= -\lambda_5 \left( h_{\beta\alpha} - h_{\alpha\beta} \right);\end{aligned}\quad (3)$$

for the first component,

$$\begin{aligned}\sigma_{\alpha\alpha}^{(2)} &= \alpha_2 + \lambda_2 e^{(2)} + 2\mu_2 \varepsilon_{\alpha\alpha}^{(2)} + \lambda_4 e^{(1)} + 2\mu_4 \varepsilon_{\alpha\alpha}^{(1)}; \\ \frac{1}{2} \left( \sigma_{\alpha\beta}^{(2)} + \sigma_{\beta\alpha}^{(2)} \right) &= 2\mu_2 \varepsilon_{\alpha\beta}^{(2)} + 2\mu_3 \varepsilon_{\alpha\beta}^{(1)}; \\ \frac{1}{2} \left( \sigma_{\alpha\beta}^{(2)} - \sigma_{\beta\alpha}^{(2)} \right) &= \lambda_5 \left( h_{\beta\alpha} - h_{\alpha\beta} \right);\end{aligned}\quad (4)$$

For the second component,  
in this case take place depending

$$\begin{aligned}\mu_4 &= \mu_3; \\ \alpha_2 &= \lambda_3 - \lambda_4\end{aligned}\quad (5)$$

here  $\alpha_2, \lambda_2, \mu_2$  elastic constants,

$$\begin{aligned}\varepsilon_{\alpha\beta}^{(j)} &= \frac{1}{2} \left( \frac{\partial U_{\alpha}^{(j)}}{\partial \beta} + \frac{\partial U_{\beta}^{(j)}}{\partial \alpha} \right); \quad (j = 1, 2); \\ h_{\alpha\beta} &= \frac{\partial U_{\alpha}^{(2)}}{\partial \beta} + \frac{\partial U_{\beta}^{(1)}}{\partial \alpha};\end{aligned}\quad (6)$$

Where  $U_\alpha^{(j)}, U_\beta^{(j)}$  the components of displacement  $\vec{U}^{(j)}$  vectors. Elastic mechanical characteristics depend on both the porosity and the adhesion conditions between the grains that make up the medium and are determined experimentally.

As can be seen from the dependences (3) and (4), the law of shear stresses does not hold, due to the mutual influence of the environmental component and other factors.

The equations of motion in stresses are:

$$\begin{aligned} \frac{\partial \sigma_{\alpha\beta}^{(1)}}{\partial \beta} - N_\alpha &= \rho_{11} \frac{\partial^2 U_\alpha^{(1)}}{\partial t^2} + \rho_{12} \frac{\partial^2 U_\alpha^{(2)}}{\partial t^2}; \\ \frac{\partial \sigma_{\alpha\beta}^{(2)}}{\partial \beta} - N_\alpha &= \rho_{12} \frac{\partial^2 U_\alpha^{(1)}}{\partial t^2} + \rho_{22} \frac{\partial^2 U_\alpha^{(2)}}{\partial t^2}, \end{aligned} \quad (7)$$

where

$$N_a = \frac{\alpha_2}{\rho} \left[ \rho_1 \frac{\partial \varepsilon^{(2)}}{\partial \alpha} + \rho_2 \frac{\partial \varepsilon^{(1)}}{\partial \alpha} \right] + \nu \left[ \frac{\partial U_\alpha^{(1)}}{\partial t} - \frac{\partial U_\alpha^{(2)}}{\partial t} \right] \quad (8)$$

$\nu$  - diffusion coefficient, and take the values (x, y, z) in a Cartesian coordinate system, or other coordinates (cylindrical, spherical, etc).

The quantities have the dimensionality of the density and are equal to:

$$\begin{aligned} \rho_1 &= \rho_{11} + \rho_{12}; \\ \rho_2 &= \rho_{22} + \rho_{12}; \\ \rho &= \rho_1 + \rho_2, \end{aligned} \quad (9)$$

wherein

$$\begin{aligned} \rho_{11}\rho_{22} - \rho_{12}^2 &> 0; \\ \rho_{12} &< 0. \end{aligned}$$

$\rho_{12}$  - plays the role of an attached mass.

If we add the left and right sides of equations (7) and introduce the notation:

$$\sigma_{\alpha\beta}^{(1)} + \sigma_{\alpha\beta}^{(2)} = \sigma_{\alpha\beta}, \quad (10)$$

then, we can take

$$\frac{\partial \sigma_{\alpha\beta}}{\partial \beta} = \rho_1 \frac{\partial^2 U_\alpha^{(1)}}{\partial t^2} + \rho_2 \frac{\partial^2 U_\alpha^{(2)}}{\partial t^2} \quad (11)$$

i.e. the total stress depends on the acceleration of the particles that make up the two-component medium.

In the case of continuous one-component medium  $U_\alpha^{(1)} = U_\alpha^{(2)}$ , from (11) we obtain the known equations:

$$\begin{aligned} \frac{\partial \sigma_{\alpha\beta}}{\partial \beta} &= \rho \frac{\partial^2 U_\alpha}{\partial t^2}; \\ (U_\alpha^{(1)} = U_\alpha^{(2)} = U_\alpha) \end{aligned} \quad (12)$$

Similarly, under conditions (12), the Hooke's law for isotropic homogeneous elastic medium is obtained from relations (3) and (4).

The equations of motion (7) are simplified by introducing potentials and longitudinal  $\Phi_j$  and  $\vec{\Psi}_j$  transverse waves.

$$\begin{aligned} \vec{U}^{(j)} &= \text{grad}\Phi_j + \text{rot}\vec{\Psi}_j; \\ \vec{\Psi}_j &= \vec{\Psi}_j(\vec{\Psi}_j^{(1)}, \vec{\Psi}_j^{(2)}, \vec{\Psi}_j^{(3)}), \end{aligned} \quad (13)$$

the solenoidal condition must be satisfied

$$\text{div}\vec{\Psi}_j = 0 \quad (j = 1, 2) \quad (14)$$

In potentials  $\Phi_j$  и  $\vec{\Psi}_j$  the equations of motion (7) are reduced to the form:

$$A_1\Delta\Phi_1 + B_1\Delta\Phi_2 = \rho_{11} \frac{\partial^2\Phi_1}{\partial t^2} + \rho_{12} \frac{\partial^2\Phi_2}{\partial t^2} + v\left(\frac{\partial\Phi_1}{\partial t} - \frac{\partial\Phi_2}{\partial t}\right); \quad (15)$$

$$A_2\Delta\Phi_2 + B_2\Delta\Phi_1 = \rho_{12} \frac{\partial^2\Phi_1}{\partial t^2} + \rho_{22} \frac{\partial^2\Phi_2}{\partial t^2} - v\left(\frac{\partial\Phi_1}{\partial t} - \frac{\partial\Phi_2}{\partial t}\right); \quad (16)$$

$$(\mu_1 - \lambda_5)\Delta\vec{\Psi}_1 + (\mu_1 + \lambda_5)\Delta\vec{\Psi}_2 = \rho_{11} \frac{\partial^2\vec{\Psi}_1}{\partial t^2} + \rho_{12} \frac{\partial^2\vec{\Psi}_2}{\partial t^2} - v\left(\frac{\partial\vec{\Psi}_1}{\partial t} - \frac{\partial\vec{\Psi}_2}{\partial t}\right); \quad (17)$$

$$(\mu_1 - \lambda_5)\Delta\vec{\Psi}_2 + (\mu_1 + \lambda_5)\Delta\vec{\Psi}_1 = \rho_{12} \frac{\partial^2\vec{\Psi}_1}{\partial t^2} + \rho_{22} \frac{\partial^2\vec{\Psi}_2}{\partial t^2} + v\left(\frac{\partial\vec{\Psi}_1}{\partial t} - \frac{\partial\vec{\Psi}_2}{\partial t}\right); \quad (18)$$

where  $\Delta$  - three-dimensional Laplace operator,

$$\begin{aligned} A_j &= \left[ \lambda_j + 2\mu_j + (-1)^j \frac{\rho_2\alpha_2}{\rho} \right]; \\ B_j &= \left[ \lambda_{j+1} + 2\mu_{j+1} + (-1)^j \frac{\rho_1\alpha_2}{\rho} \right]; \end{aligned} \quad (19)$$

and constants  $\lambda_j, \mu_j$  must satisfy the inequalities [3]:

$$\begin{aligned} A_1; A_2 &\neq (B_1^2; B_2^2); \\ (A_1 + \mu_1)(A_2 + \mu_2) - (B_{1,2} + \mu_3)^2 &\neq 0 \\ \mu_1\mu_2 &\neq \mu_3^2; \\ (\lambda_1 + \mu_1)(\lambda_2 + \mu_2) &\neq (\lambda_3 + \mu_3)(\lambda_4 + \mu_4). \end{aligned}$$

In the absence of diffusion, i.e. for  $v = 0$ , in the equations (15), (16) and (17), (18) we set

$$\begin{aligned} \Phi_1 &= \varphi; \quad \Phi_2 = \gamma\varphi; \\ \vec{\Psi}_1 &= \vec{\psi}_1; \quad \vec{\Psi}_2 = \delta\vec{\psi} \end{aligned} \quad (20)$$

Substituting (20) into equations (15.) - (18.), to determine and obtain algebraic equations;

$$(B_1\rho_{22} - A_2\rho_{12})\gamma^2 + [(B_1 - B_2)\rho_{12} + (A_1\rho_{22} - A_2\rho_{11})]\gamma - (-A_1\rho_{12} + B_2\rho_{11}) = 0; \quad (21)$$

$$\begin{aligned} [(\mu_3 + \lambda_5)\rho_{22} - (\mu_2 - \lambda_5)\rho_{12}]\delta^2 + [(\mu_1 + \lambda_5)\rho_{22} - (\mu_2 - \lambda_5)\rho_{11}]\delta - \\ - [(\mu_3 + \lambda_5)\rho_{11} - (\mu_1 - \lambda_5)\rho_{12}] = 0 \end{aligned} \quad (22)$$

As it can be seen from equations (21) and (22), they have two real roots, which we denote by  $(\gamma_1, \gamma_2)$  and  $(\delta_1, \delta_2)$ .

Hence, by the principle of superposition can be put;

$$\begin{aligned} \Phi_1 &= \varphi_1 + \varphi_2; \\ \Phi_2 &= \lambda_1 \varphi_1 + \lambda_2 \varphi_2; \\ \Psi_1 &= \psi_1 + \psi_2; \\ \Psi_2 &= \delta_1 \psi_1 + \delta_2 \psi_2; \end{aligned} \tag{23}$$

And for  $\varphi_1$  и  $\vec{\psi}_1$  we obtain separate wave equations:

$$\Delta \varphi_j = \frac{1}{a_j^2} \frac{\partial^2 \varphi_j}{\partial t^2}; \quad (j=1,2) \tag{24.}$$

$$\Delta \vec{\psi} = -\frac{1}{b_j^2} \frac{\partial^2 \vec{\psi}_o}{\partial t^2}; \quad (j=1,2) \tag{25}$$

while generalized velocities  $a_j, b_j$  longitudinal and transverse waves are equal:

$$\begin{aligned} a_j^2 &= \frac{A_1 + \gamma_j B_1}{\rho_{11} + \gamma_j \rho_{12}} = \frac{A_2 \gamma_j + B_2}{\rho_{12} + \gamma_j \rho_{22}}; \quad (j=1,2) \\ b_j^2 &= \frac{(\mu_1 - \lambda_5) + (\mu_3 + \lambda_5) \delta_j}{\rho_{11} + \gamma_j \rho_{12}} = \frac{(\mu_2 - \lambda_5) \delta_j + (\mu_3 + \lambda_5)}{\rho_{12} + \gamma_j \rho_{22}}; \end{aligned} \tag{26}$$

$(j=1,2)$

In the presence of diffusion, the system of equations (15) - (18) does not reduce to separate equations of the type (24) - (25).

Let us consider a porous elastic medium with liquid filler with an imperfect bond between the elastic skeleton and the reservoir.

Dependencies between strains and stresses are more conveniently written in the form

$$\begin{aligned} \sigma_{\alpha\beta} &= 2\mu\varepsilon_{\alpha\beta} + \delta_{\alpha\beta}(\lambda\varepsilon + Q\varepsilon_0); \\ \sigma &= Q\varepsilon + R\varepsilon_0; \quad \sigma = -RK_0 \end{aligned} \tag{27}$$

where  $\varepsilon_{\alpha\beta}$  - deformation of the skeleton.

$$\varepsilon = \varepsilon_{xx} = \varepsilon_{yy} = \varepsilon_{zz}$$

$\varepsilon_0$  – volumetric deformation of liquid filler;  $\lambda, \mu, Q, R$  – mechanical characteristics of a two-component medium;  $P$  – pressure in the liquid component.

There are types of the equations of motion in stresses:

$$\begin{aligned} \frac{\partial \sigma_{\alpha\beta}}{\partial \beta} &= \rho_{11} \frac{\partial^2 U_{\alpha}^{(1)}}{\partial t^2} + \rho_{22} \frac{\partial^2 U_{\alpha}^{(2)}}{\partial t^2}; \\ \frac{\partial \sigma}{\partial \beta} &= \rho_{12} \frac{\partial^2 U_{\alpha}^{(1)}}{\partial t^2} + \rho_{22} \frac{\partial^2 U_{\alpha}^{(2)}}{\partial t^2}. \end{aligned} \tag{28}$$

wherein  $\alpha$  and  $\beta$  run through values in the Cartesian coordinate system and dependencies  $(x, y, z)$  and dependencies must be fulfilled (18).

Equations of motion (28) are simplified by introducing potentials  $\Phi_j, \vec{\Psi}_j$  by formulas (13), wherein  $\vec{\Psi}_j$  must satisfy condition (14).

In the potentials of equation  $\Phi_j, \vec{\Psi}_j$  motion (28) are reduced to the form:

$$\begin{aligned}
 (\lambda + 2\mu)\Delta\Phi_1 + Q\Phi_2 &= \rho_{11} \frac{\partial^2\Phi_1}{\partial t^2} + \rho_{12} \frac{\partial^2\Phi_2}{\partial t^2}; \\
 Q\Delta\Phi_1 + R\Delta\Phi_2 &= \rho_{12} \frac{\partial^2\Phi_1}{\partial t^2} + \rho_{22} \frac{\partial^2\Phi_2}{\partial t^2}; \\
 \mu\Delta\bar{\Psi}_1 &= \frac{(\rho_{11}g_{22} - \rho_{12}^2)}{\rho_{22}} \frac{\partial^2\bar{\Psi}_1}{\partial t^2} + \rho_{22} \frac{\partial^2\bar{\Psi}_2}{\partial t^2}; \\
 \frac{\partial^2\bar{\Psi}_2}{\partial t^2} &= -\frac{\rho_{12}}{\rho_{22}} \frac{\partial^2\bar{\Psi}_1}{\partial t^2};
 \end{aligned} \tag{29}$$

thinking

$$\Phi_1 = \varphi; \quad \Phi_2 = \gamma\varphi \tag{30}$$

and substituting (30) in the first two equations (29), we obtain  $\gamma$  the following equation for the determination:

$$\gamma^2 + \frac{(\lambda + 2\mu)\rho_{22} - R\rho_{11}}{\rho_{22}Q - \rho_{12}R} \gamma - \frac{\rho_{11}Q - (\lambda + 2\mu)\rho_{12}}{\rho_{22}Q - \rho_{12}R} = 0 \tag{31}$$

which has two real roots  $\gamma_1$  и  $\gamma_2$ . Consequently,

$$\Phi_1 = \varphi_1 + \varphi_2; \quad \Phi_2 = \gamma_1\varphi_1 + \gamma_2\varphi_2 \tag{32}$$

and potentials  $\varphi_1, \varphi_2$  satisfy the wave equations:

$$\Delta\varphi_j = \frac{1}{a_j^2} \frac{\partial^2\varphi_j}{\partial t^2} \quad (j = 1, 2) \tag{33}$$

where the generalized velocities  $a_j$  are:

$$a_j^2 = \frac{(\lambda + 2\mu)Q\gamma_j}{\rho_{11} + \rho_{12}\gamma_j}; \tag{34}$$

The last two of equations (29) can conveniently be reduced to the form:

$$\Delta\bar{\Psi}_1 = \frac{1}{b^2} \frac{\partial^2\bar{\Psi}_1}{\partial t^2}; \quad \bar{\Psi}_2 = -\frac{\rho_{12}}{\rho_{22}} \bar{\Psi}_1 \tag{35}$$

wherein

$$b^2 = \frac{\mu\rho_{22}}{\rho_{11}\rho_{22} - \rho_{12}^2}; \tag{36}$$

In the generalized potentials, the values of displacements will be written as:

$$\begin{aligned}
 U_x^{(1)} &= \frac{\partial}{\partial x}(\varphi_1 + \varphi_2) + \frac{\partial\Psi_3^{(1)}}{\partial y} - \frac{\partial\Psi_2^{(1)}}{\partial z}; \\
 U_x^{(2)} &= \frac{\partial}{\partial x}(\gamma_1\varphi_1 + \gamma_2\varphi_2) + \frac{\partial\Psi_3^{(3)}}{\partial y} - \frac{\partial\Psi_2^{(2)}}{\partial z}; \\
 U_y^{(1)} &= \frac{\partial}{\partial y}(\varphi_1 + \varphi_2) + \frac{\partial\Psi_1^{(1)}}{\partial z} - \frac{\partial\Psi_3^{(1)}}{\partial x};
 \end{aligned}$$

$$\begin{aligned}
 U_y^{(1)} &= \frac{\partial}{\partial y} (\gamma_1 \varphi_1 + \gamma_2 \varphi_2) + \frac{\partial \Psi_1^{(2)}}{\partial z} - \frac{\partial \Psi_3^{(2)}}{\partial x}; \\
 U_z^{(1)} &= \frac{\partial}{\partial z} (\varphi_1 + \varphi_2) + \frac{\partial \Psi_2^{(1)}}{\partial x} - \frac{\partial \Psi_1^{(1)}}{\partial y}; \\
 U_z^{(1)} &= \frac{\partial}{\partial z} (\gamma_1 \varphi_1 + \gamma_2 \varphi_2) + \frac{\partial \Psi_2^{(2)}}{\partial x} - \frac{\partial \Psi_1^{(2)}}{\partial y};
 \end{aligned} \tag{37}$$

For a two-component elastic medium with  $\nu = 0$ :

$$\Psi_i^{(j)} = \delta_1 \Psi_i^{(j)} + \delta_2 \Psi_i^{(j)} \tag{38}$$

and for two-component porous media

$$\Psi_i^{(2)} = -\frac{\rho_{12}}{\rho_{22}} \Psi_i^{(1)} \tag{39}$$

The deformation and stress of two-component media are determined through the displacement (37) according to the known formulas and generalized Hooke's laws (3), (4) and (27).

Plane generalized stress state is used in the study of wave processes in bounded media such as plates. It is approximately formulated under the condition that the unknown quantities are independent of the transverse coordinates  $z$ , i.e. when

$$U_{1z} = U_{2z} \approx 0 \tag{40}$$

In this case from (27)

$$\varepsilon_{zz} = -\left[ \frac{\lambda}{\lambda + 2\mu} (\varepsilon_{xx} + \varepsilon_{yy}) + \frac{Q}{\lambda + 2\mu} \varepsilon_0 \right] \tag{41}$$

and relations (17) have type:

$$\begin{aligned}
 \sigma_{xx} &= \frac{4\mu(\lambda + \mu)}{(\lambda + 2\mu)} \varepsilon_{xx} + \frac{2\mu\lambda}{(\lambda + 2\mu)} \varepsilon_{yy} + \frac{2\mu Q}{(\lambda + 2\mu)} \varepsilon_0; \\
 \sigma_{xx} &= \frac{2\mu\lambda}{(\lambda + 2\mu)} \varepsilon_{xx} + \frac{4\mu(\lambda + \mu)}{(\lambda + 2\mu)} \varepsilon_{yy} + \frac{2\mu Q}{(\lambda + 2\mu)} \varepsilon_0; \\
 \sigma_{xy} &= \mu \varepsilon_{xy}; \\
 \sigma &= Q\varepsilon + R\varepsilon_0;
 \end{aligned} \tag{42}$$

wherein:

$$\begin{aligned}
 \varepsilon &= \varepsilon_{xx} + \varepsilon_{yy}; \quad \varepsilon_0 = \varepsilon_{xx}^{(0)} + \varepsilon_{yy}^{(0)}; \\
 \varepsilon_{xx} &= \frac{\partial U_1}{\partial x}; \quad \varepsilon_{xy} = \frac{\partial U_1}{\partial y} + \frac{\partial U_1}{\partial x}; \\
 \varepsilon_{xx}^{(0)} &= \frac{\partial U_2}{\partial x}; \quad \varepsilon_{yy}^{(0)} = \frac{\partial U_2}{\partial y};
 \end{aligned} \tag{43}$$

We write the equations of motion in the form:

$$\begin{aligned}
 \frac{\partial \sigma_{xx}}{\partial x} + \frac{\partial \sigma_{xy}}{\partial y} &= \rho_{11} \frac{\partial^2 U_1}{\partial t^2} + \rho_{12} \frac{\partial^2 U_2}{\partial t^2}; \\
 \frac{\partial \sigma_{xy}}{\partial x} + \frac{\partial \sigma_{yy}}{\partial y} &= \rho_{11} \frac{\partial^2 U_1}{\partial t^2} + \rho_{22} \frac{\partial^2 U_2}{\partial t^2}; \\
 \frac{\partial \sigma}{\partial x} &= \rho_{12} \frac{\partial^2 U_1}{\partial t^2} + \rho_{22} \frac{\partial^2 U_2}{\partial t^2}; \\
 \frac{\partial \sigma}{\partial y} &= \rho_{12} \frac{\partial^2 U_1}{\partial t^2} + \rho_{22} \frac{\partial^2 U_2}{\partial t^2};
 \end{aligned}
 \tag{44}$$

Equations (44) can be reduced to a system of wave equations, assuming:

$$\begin{aligned}
 U_1 &= \frac{\partial \varphi_1}{\partial x} + \frac{\partial \Psi_1}{\partial y}; & U_2 &= \frac{\partial \varphi_2}{\partial x} + \frac{\partial \Psi_2}{\partial y} \\
 V_1 &= \frac{\partial \varphi_1}{\partial y} - \frac{\partial \Psi_1}{\partial x}; & V_2 &= \frac{\partial \varphi_2}{\partial y} - \frac{\partial \Psi_2}{\partial x};
 \end{aligned}
 \tag{45}$$

The model of the simultaneous generalized stress state is used in the study of one-dimensional waves in bounded media such as rods of rectangular cross-section.

The theory of transversally isotropic prestressed porous two-component medium is formulated for an infinite layer of finite thickness that is in space  $(x, y, z)$ , and the medium is bounded on the coordinate.

On the basis of the mathematical theory of oscillations of elastic or viscoelastic plate under nonstationary external actions, exact equations of longitudinal and transverse vibrations of viscoelastic plates are derived with and without allowance for initial displacements and stresses, approximate equations for the physical nonlinearity of the material. For such problems, expressions are obtained for all displacements and stresses along the thickness of the plate and basic boundary problems are formulated, leading to longitudinal or transverse vibrations of the plate. On the basis of exact equations some approximate equations that follow from them with some degree of accuracy are analyzed and approximate boundary value problems are formulated for them.

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### **СТАЦИОНАРЛЫҚ ЕМЕС ІШКІ ӘСЕР КЕЗІНДЕГІ ҚАТТЫ НЕМЕСЕ СОЗЫЛМАЛЫ-ҚАТТЫ ПЛАСТИНКАЛАРДЫҢ МАТЕМАТИКАЛЫҚ ТЕРБЕЛІС ТЕОРИЯСЫ**

**Аннотация.** Бұл жұмыста автор стационарлы емес сыртқы әсерлер кезінде иілгіш және тұтқыр иілгіш пластиналардың динамикалық қозғалысын анықтау дірілдерін математикалық теория тұрғысынан түсіндіруге талпынған. Осы көзқарасқа негізделген физикалық бейсызықтық материалдар теңдеулеріне жақындатылған, бастапқы ауыстыру мен кернеулерді ескерген және ескерусіз тұтқыр иілгіш пластиналардың бойлық және көлденең дірілдерінің нақты теңдеулері шығарылған. Пластиналардың қалыңдығы бойынша барлық кернеу мен ауыстырулар үшін есептер қарастырылған және де пластиналардың бойлық және көлденең дірілдеріне алып келетін негізгі шектік есептер құрастырылған. Нақты теңдеулер негізінде сол немесе олардан кейінгі дәлдік дәрежесі бар кейбір жуықтау теңдеулері талданған және олар үшін шекаралық есептер құрастырылған.

**Түйін сөздер:** упругий, вязкоупругий, нестационарный, колебания, нелинейный, деформируемый, продольный, поперечный.

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### **МАТЕМАТИЧЕСКАЯ ТЕОРИЯ КОЛЕБАНИЙ УПРУГИХ ИЛИ ВЯЗКОУПРУГИХ ПЛАСТИН ПРИ НЕСТАЦИОНАРНЫХ ВНЕШНИХ ВОЗДЕЙСТВИЯХ**

**Аннотация.** В настоящей работе предпринята попытка изложения математической теории колебаний упругой или вязкоупругой пластинки для изучения динамического их поведения при нестационарных внешних воздействиях. На основе такого подхода выведены точные уравнения продольных и поперечных колебаний вязкоупругих пластин с учетом и без учета начальных смещений и напряжений, приближенные уравнения физической нелинейности материала. Для всех задач получены выражения для всех смещений и напряжений по толщине пластинки и сформулированы основные краевые задачи, приводящие к продольному или поперечному колебаниям пластинки. На основе точных уравнений проанализированы некоторые вытекающие из них приближенные уравнения с той или иной степенью точности и сформулированы для них приближенные краевые задачи.

**Ключевые слова:** упругий, вязкоупругий, нестационарный, колебания, нелинейный, деформируемый, продольный, поперечный.

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**ISSN 2518-170X (Online), ISSN 2224-5278 (Print)**

<http://geolog-technical.kz/index.php/kz/>

Верстка Д. Н. Калкабековой

Подписано в печать 08.12.2017.

Формат 70x881/8. Бумага офсетная. Печать – ризограф.

19,0 п.л. Тираж 300. Заказ 6.